


HW

Handlebody Decomposition



Problems

① Draw a handlebody decomposition of

① a) T^2

② b) Σ_2

③ c) $IRIP^2$

② Determine the number of each k -handle for

① $\mathbb{R}P^n$

② $\mathbb{C}P^n$

$$\mathbb{C}P^n = \mathbb{C}^{n+1} - \{0\} / z \sim w$$

$$z \sim w \iff w = \lambda z \quad \text{for some } \lambda \in \mathbb{C}^{n+1} - \{0\}$$

i.e.

$z \sim w \iff$ they are complex linearly DEP.

Q: What is $\mathbb{C}P^1$?